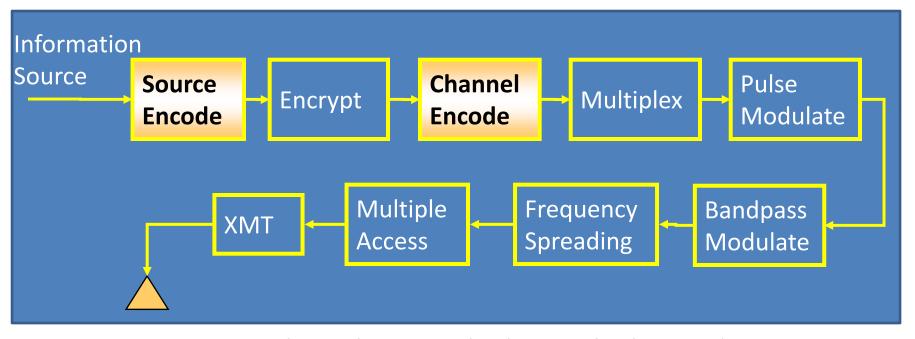
Source Coding

Overview



Source Coding – eliminate redundancy in the data, send same information in fewer bits

Channel Coding – Detect/Correct errors in signaling and improve BER

Source Coding

- Goal is to find an efficient description of information sources
 - Reduce required bandwidth
 - Reduce memory to store
- Memoryless –If symbols from source are independent, one symbol does not depend on next
- Memory elements of a sequence depend on one another, e.g. UNIVERSIT_?, 10-tuple contains less information since dependent

$$H(X)_{memory} < H(X)_{no\ memory}$$

Source Coding (II)

$$H(X)_{memory} < H(X)_{no\ memory}$$

 This means that it's more efficient to code information with memory as groups of symbols

Desirable Properties

- Length
 - Fixed Length ASCII
 - Variable Length Morse Code, JPEG
- Uniquely Decodable allow user to invert mapping to the original
- Prefix-Free No codeword can be a prefix of any other codeword
- Average Code Length (n_i is code length of ith symbol)

$$\overline{n} = \sum_{i} n_i P(X_i)$$

Uniquely Decodable and Prefix Free Codes

Uniquely decodable?

- Not code 1
- If "10111" sent, is code 3 'babbb'or 'bacb'? Not code 3 or 6

X_i	$P(X_i)$
a	0.73
b	0.25
C	0.02

Prefix-Free

- Not code 4,
- prefix contains '1'

Avg Code Length

- Code 2: n=2
- Code 5: n=1.23

Sym bol	Code 1	Code 2	Code 3	Code 4	Code 5	Code 6
a	00	00	0	1	1	1
b	00	01	1	10	00	01
c	11	10	11	100	01	11

Huffman Code

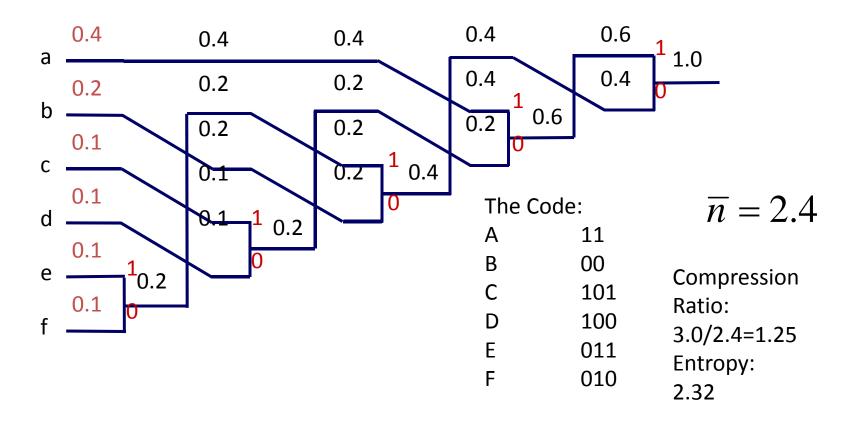
Characteristics of Huffman Codes:

- Prefix-free, variable length code that can achieve the shortest average code length for an alphabet
- Most frequent symbols have short codes

Procedure

- List all symbols and probabilities in descending order
- Merge branches with two lowest probabilities, combine their probabilities
- Repeat until one branch is left

Huffman Code Example



Example:

 Consider a random vector X = {a, b, c} with associated probabilities as listed in the Table

X_i	$P(X_i)$
a	0.73
b	0.25
c	0.02

- Calculate the entropy of this symbol set
- Find the Huffman Code for this symbol set
- Find the compression ratio and efficiency of this code

Extension Codes

- Combine alphabet symbols to increase variability
- Try to combine very common 2,3 letter combinations, e.g.: th,sh, ed, and, the,ing,ion

```
\overline{n} = 1.9326 \ bits / 2 symbols
```

=0.9663	bit /	' symb	pol
---------	-------	--------	-----

X_i	$P(X_i)$
aa	0.5329
ab	0.1825
ba	0.1825
bb	0.0625
ac	0.0146
ca	0.0146
bc	0.0050
cb	0.0050
cc	0.0002

Code	n_i	$n_i P(X_i)$
1	1	0.5329
00	2	0.3650
011	3	0.5475
0101	4	0.2500
01000	5	0.0730
010011	6	0.0876
0100100	7	0.0350
01001011	8	0.0400
01001010	8	0.0016

Lempel-Ziv (ZIP) Codes

- Huffman codes have some shortcomings
 - Know symbol probability information a priori
 - Coding tree must be known at coder/decoder
- Lempel-Ziv algorithm use text itself to iteratively construct a sequence of variable length code words
- Used in gzip, UNIX compress, LZW algorithms

Lempel-Ziv Algorithm

- Look through a code dictionary with already coded segments
 - If matches segment,
 - send <dictionary address, next character> and store segment + new character in dictionary
 - If no match,
 - store in dictionary, send <0,symbol>

LZ Coding: Example

Encode [abaababbbbbbbbbbbbbb]

Code Diction Address Co	•	Encoded Packets	
1	а	< 0 , a >	Note: 9 code
2	b	< 0 , b >	words, 3 bit
3	aa	<1,a>	address, 1 bit
4	ba	< 2 , a >	for new
5	bb	< 2 , b >	character,
6	bbb	<5,b>	
7	bba	< 5 , a >	
8	bbbb	< 6 , b >	
		< 4 , ->	